

# Insights from O-C study of 7000+ Magellanic Cepheids from OGLE survey: Census of irregular period changes and binary Cepheids candidates

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Based on Rathour et al. 2023(a, b) [in prep.]

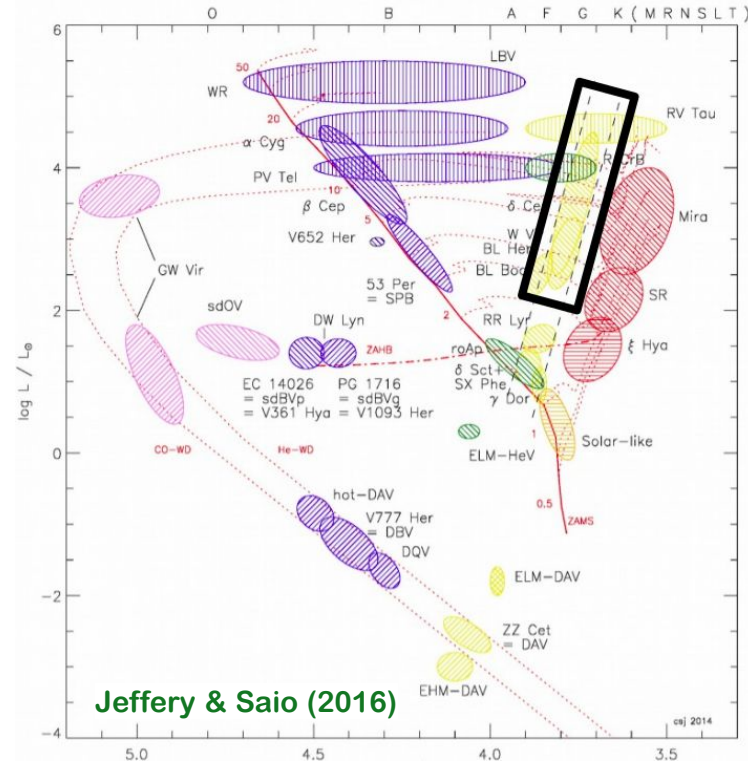


# CEPHEIDS

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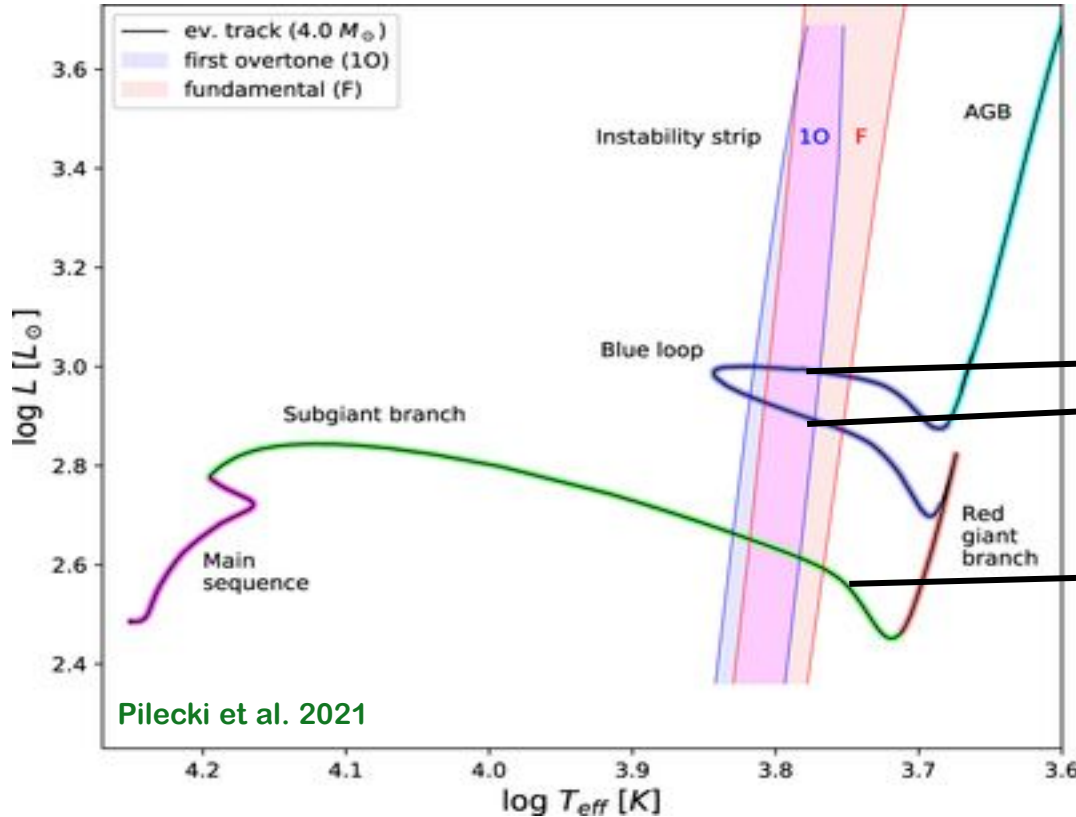
- Classical pulsators evolved from main-sequence  
Period: 1–100 days  
Mass: ~3–13  $M_{\odot}$   
Mv: -0.2
- Excellent for extragalactic distance measurements
- Perfect for stellar evolution and pulsation studies



# PERIOD CHANGES IN CEPHEIDS

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# Period change (PC) and Crossing Number



$$\text{Period - Mean Density Relation: } \Pi \sim \sqrt{1/\bar{\rho}} \sim R^{3/2} M^{-1/2}$$

Core Helium burning  
(Slow)

Hydrogen exhaustion at the core  
Shell hydrogen burning  
(Fast)

# Taxonomy of PC

Evolutionary  
( $\sim 10^4 - 10^7$  yr)

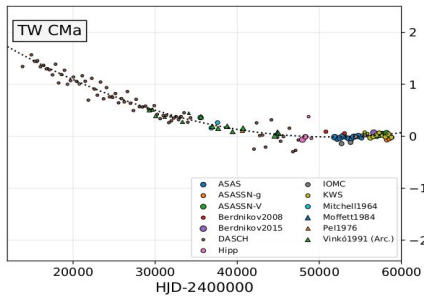
Non-evolutionary  
( $\sim 10^3$  days)

Positive

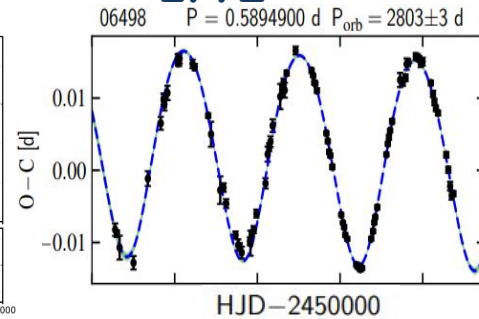
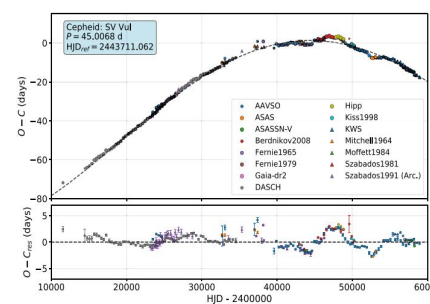
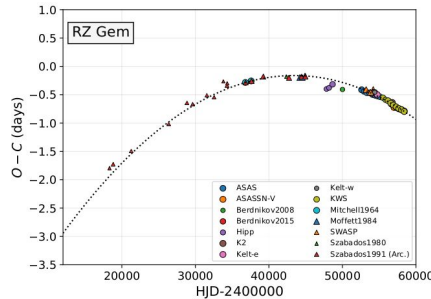
Negative

Irregular

LTTE



G. Csörnyei et al. (2021)



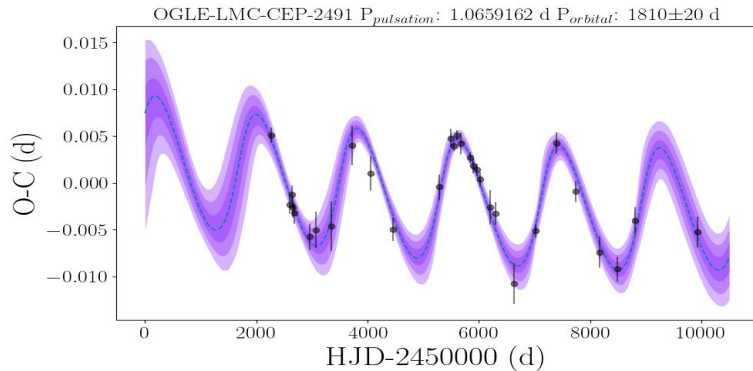
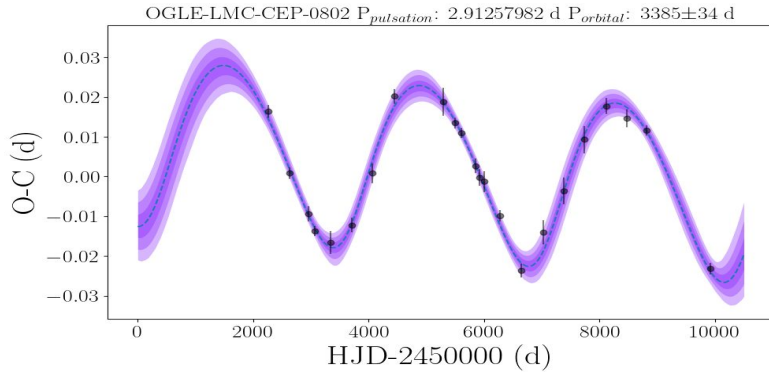
G. Hajdu et al. (2021)

# FINDINGS I: CEPHEIDS IN BINARY SYSTEMS

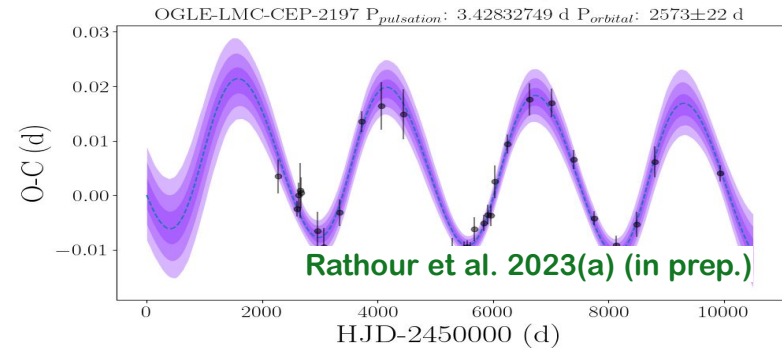
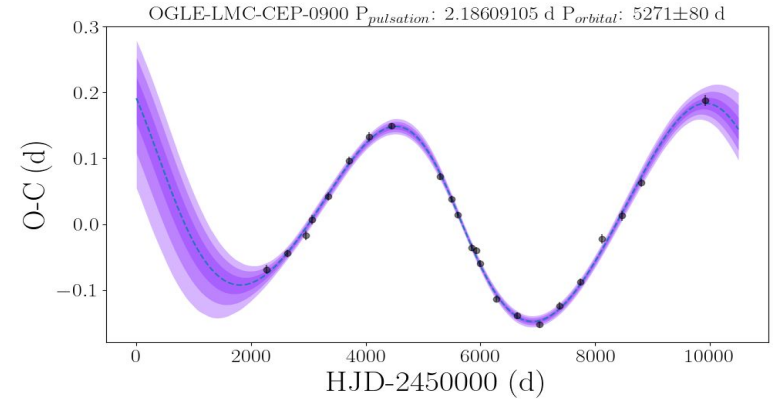
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# LMC Binary candidates

## Fundamental



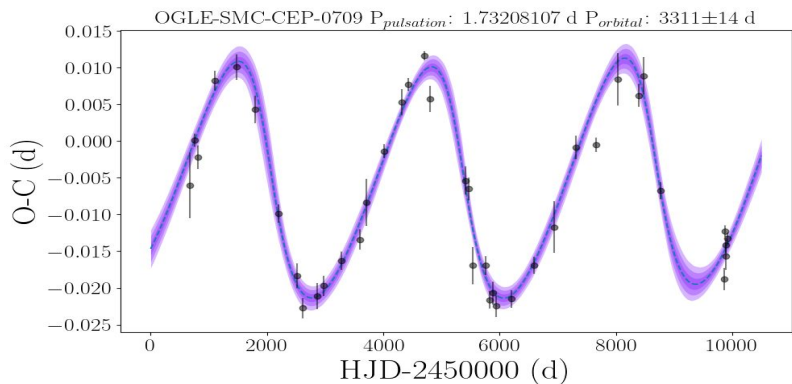
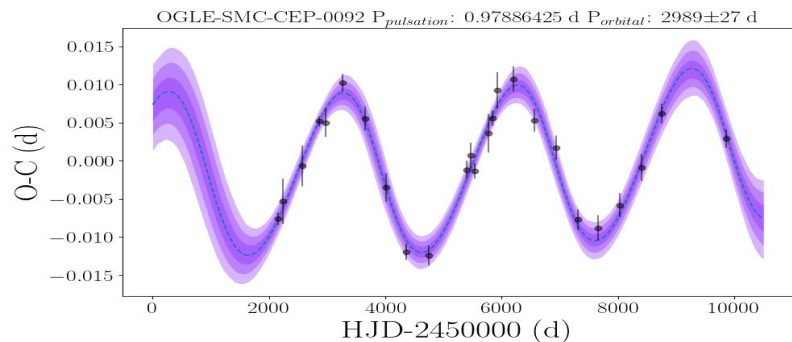
## Overtone



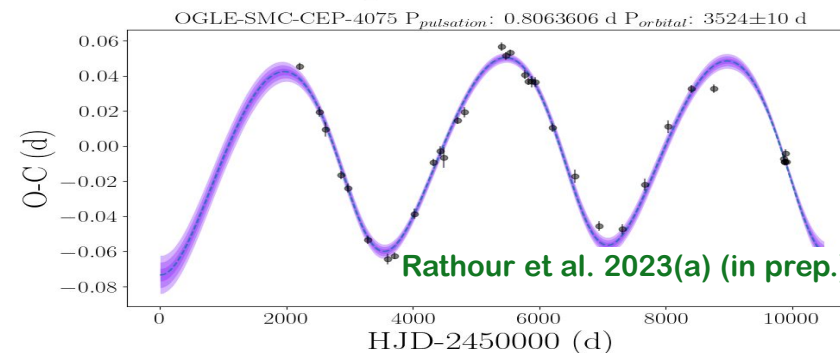
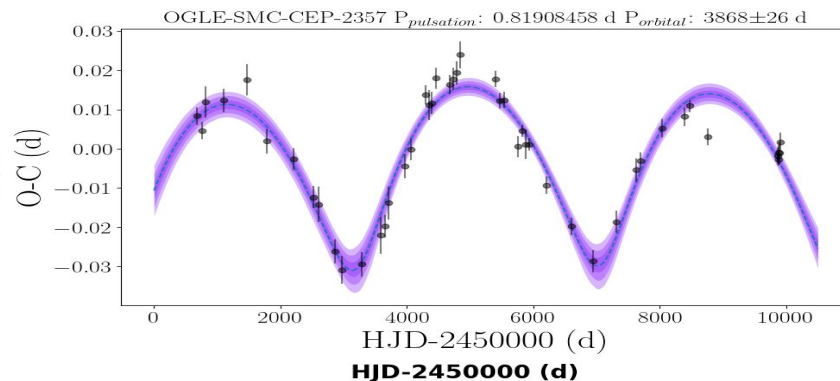


# SMC Binary candidates

## Fundamental



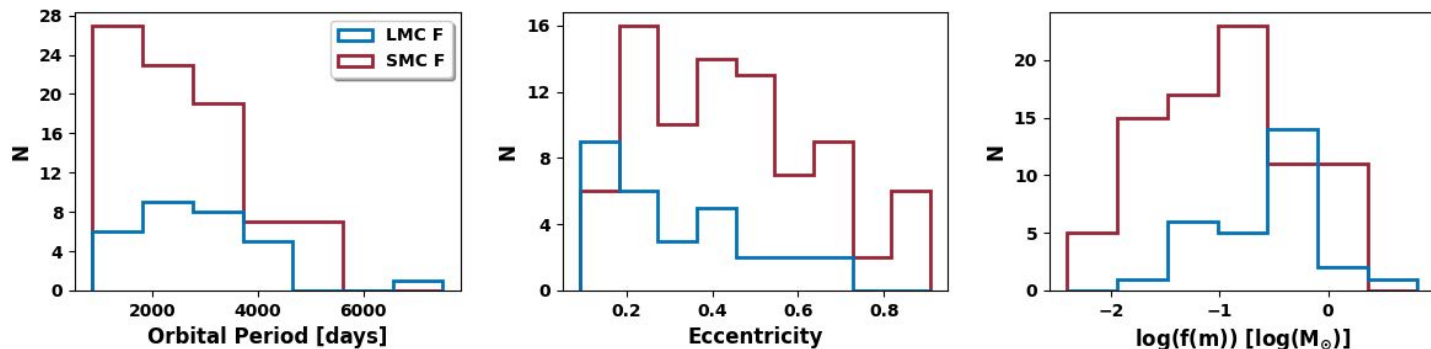
## Overtone



# BINARY STATISTICS

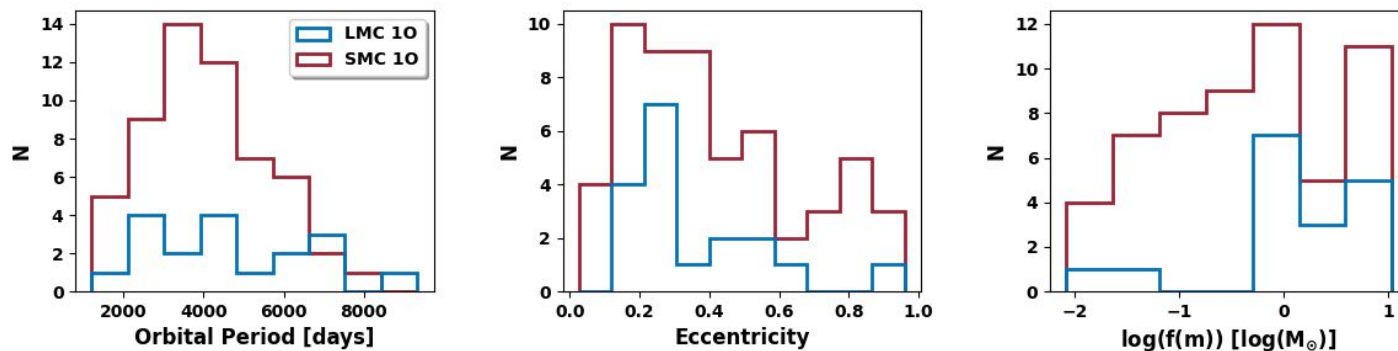
|                          | LMC F   | LMC 10  | SMC F   | SMC 10  |
|--------------------------|---------|---------|---------|---------|
| Starting sample:         | 1801    | 1238    | 2582    | 1617    |
| O-C + visual inspection: | 39      | 52      | 102     | 133     |
| Binary parameters:       | 30      | 22      | 85      | 60      |
| Fraction:                | ~1.67 % | ~1.77 % | ~3.29 % | ~3.72 % |

# RESULTS: LMC vs SMC



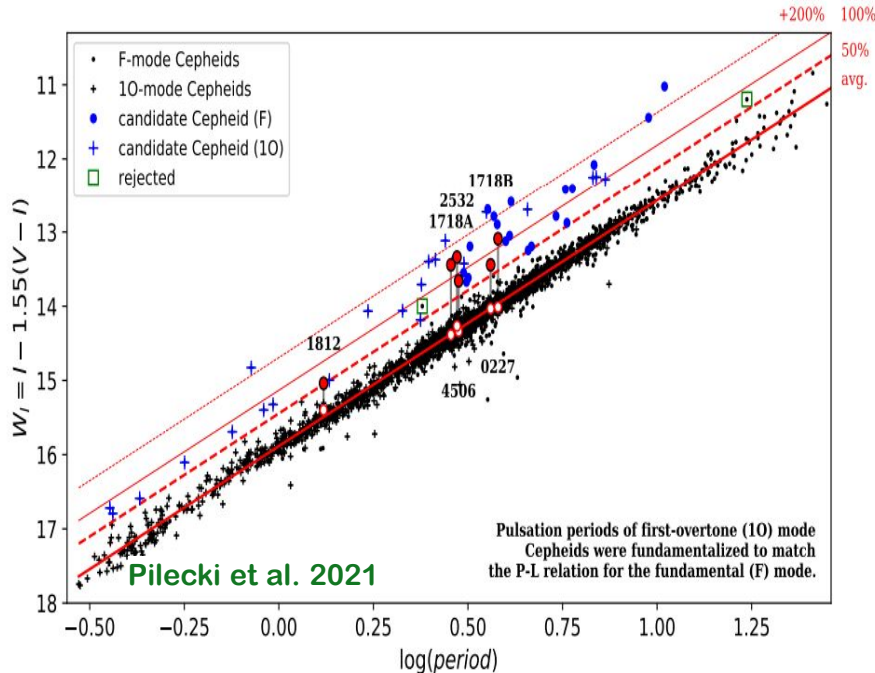
Median companion mass:  $1.38 M_{\odot}$  LMC;  $0.96 M_{\odot}$  SMC

# RESULTS: LMC vs SMC



Median companion mass:  $2.71 M_{\odot}$  LMC;  $1.36 M_{\odot}$  SMC

# Finding companions with Period-Wesenheit relation?

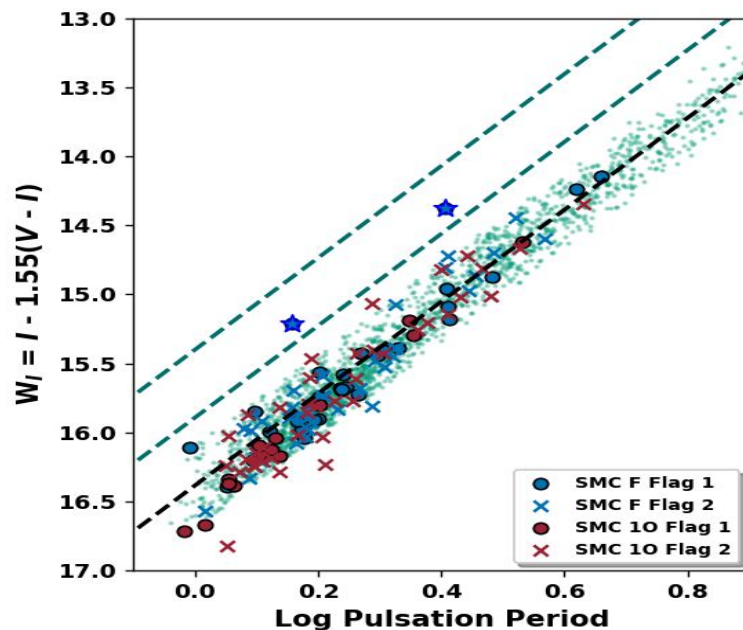
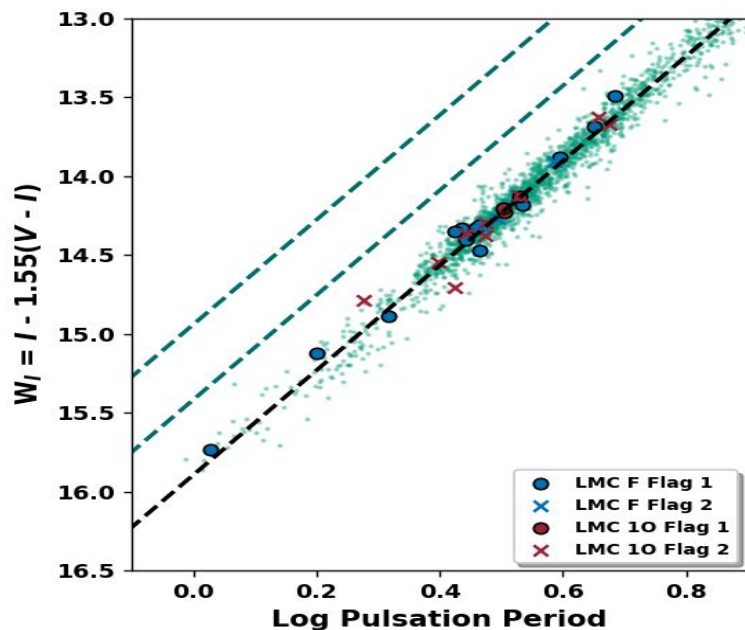


## 2. The Hypothesis

As described above, there is a great need for an independent source of Cepheids in binary systems that are well suited for mass determination. The most valuable would be those in double-lined spectroscopic binaries, for which lines of both components are present in the spectra. To meet these conditions, one has to find Cepheids accompanied by stars of similar luminosity, and preferentially of late spectral types, i.e., at a subgiant or later stage of evolution. To identify them, we can consider at least three observable features caused by such companions:

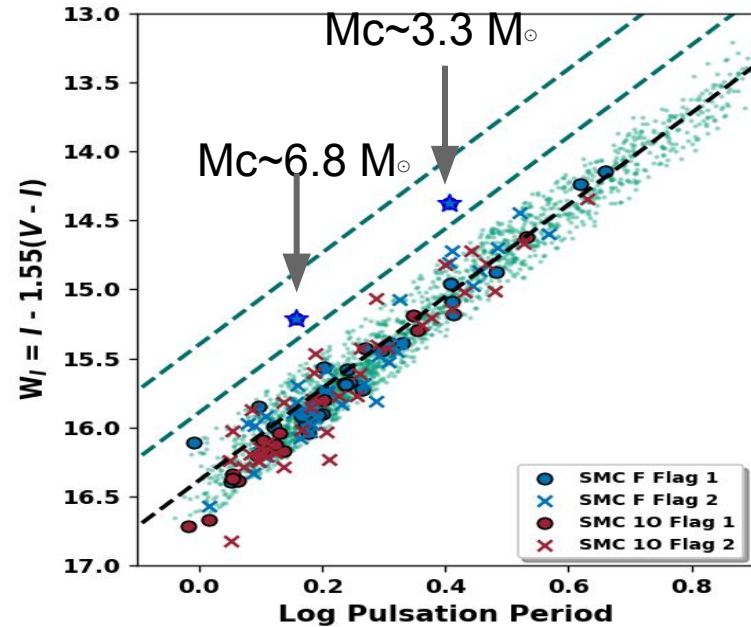
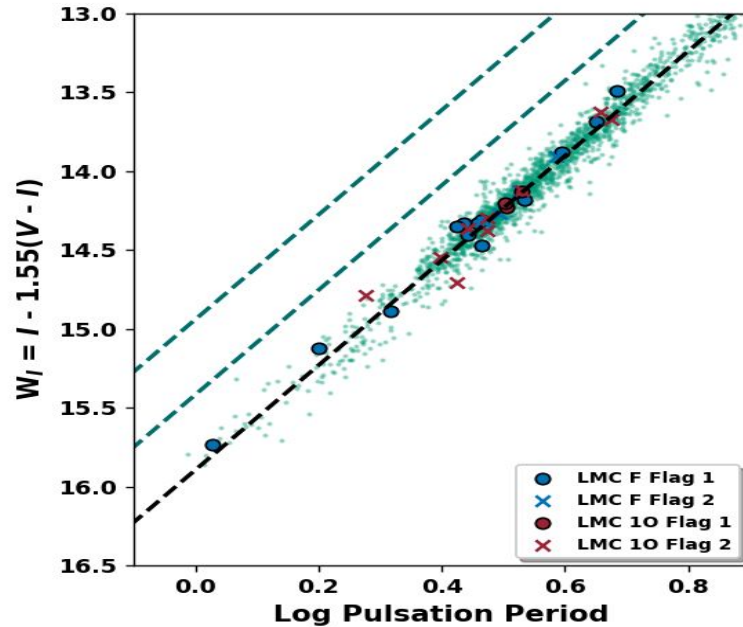
1. the total observed brightness of a Cepheid should increase significantly;
2. its photometric pulsation amplitude (expressed in magnitudes) should decrease;
3. its color should be either similar or redder (we expect companions mostly on the red giant branch or the blue loop).

# Finding companions with Period-Wesenheit relation?



Rathour et al. 2023(a) (in prep.)

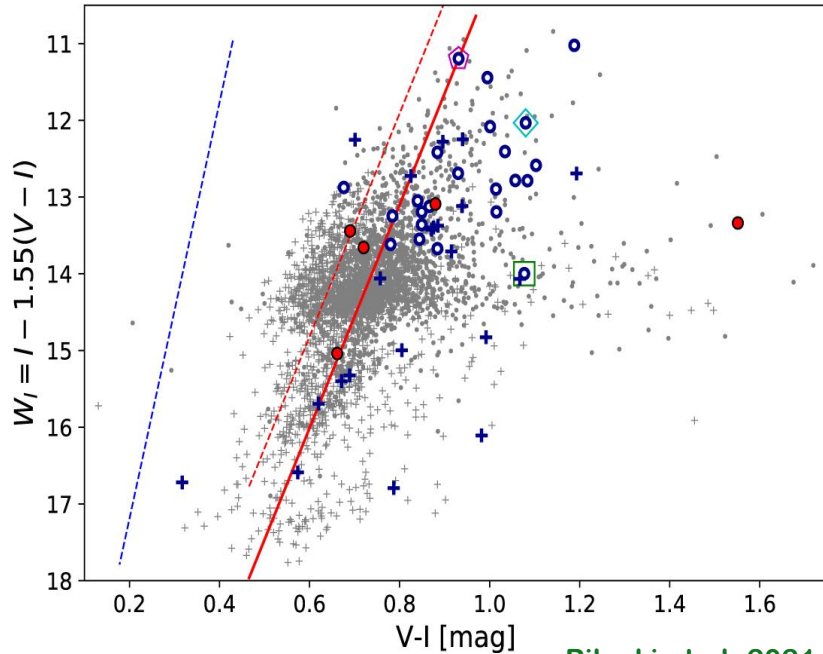
# Finding companions with Period-Wesenheit relation?



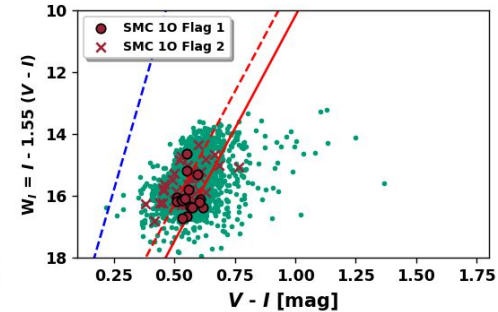
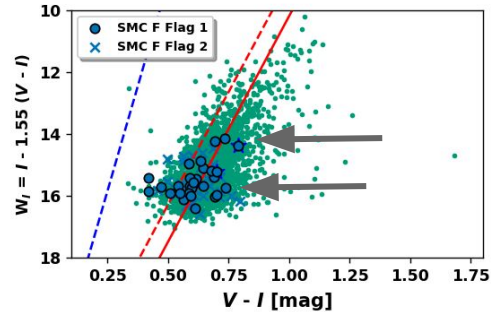
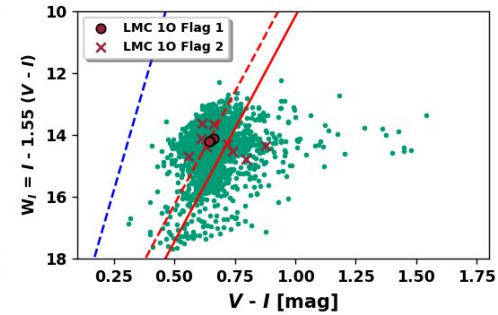
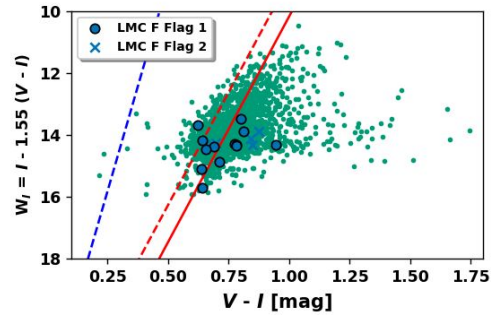
Rathour et al. 2023(a) (in prep.)



# Color-Wesenheit Diagram



Pilecki et al. 2021



Rathour et al. 2023(a) (in prep.)

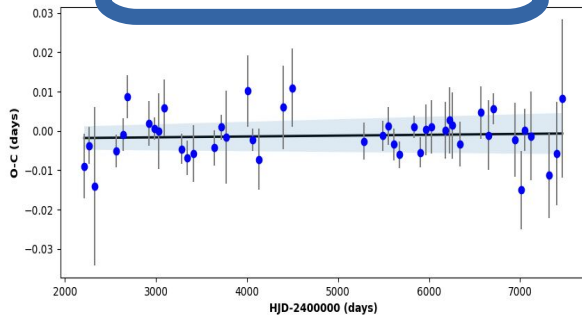


# **FINDINGS II: CEPHEIDS WITH IRREGULAR PERIOD CHANGES**

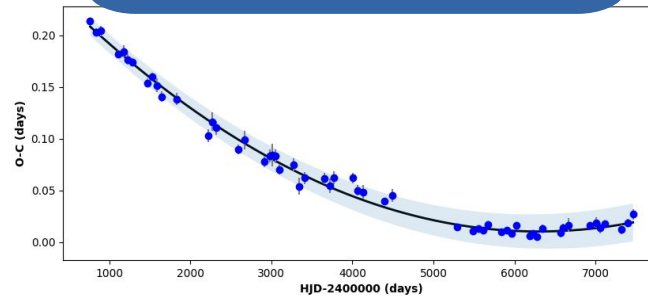
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# Classification

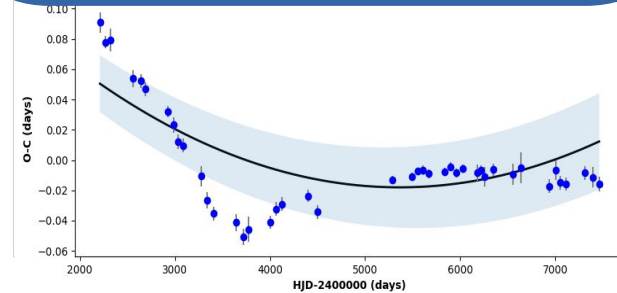
No period change



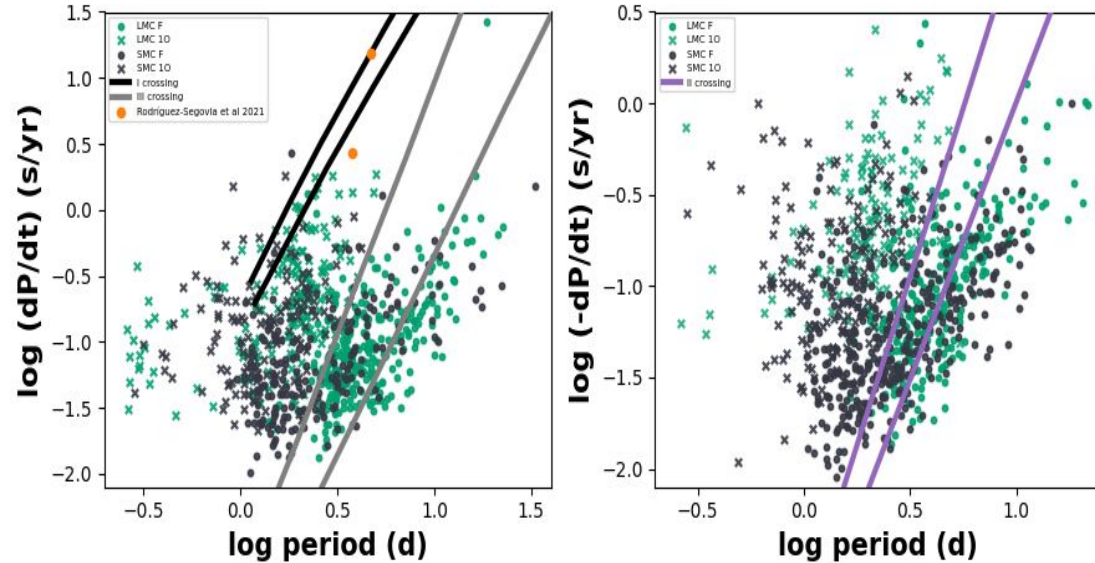
Linear period change



Non-Linear period change

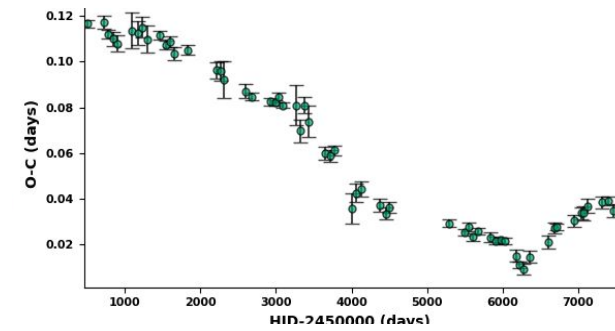
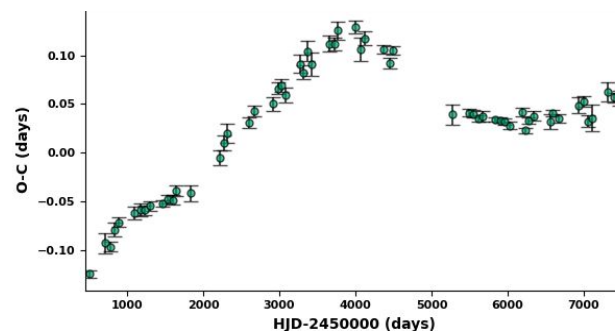
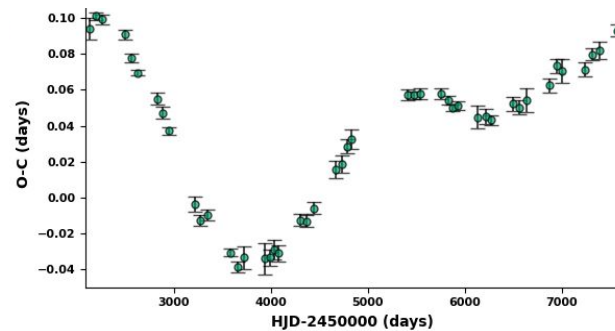
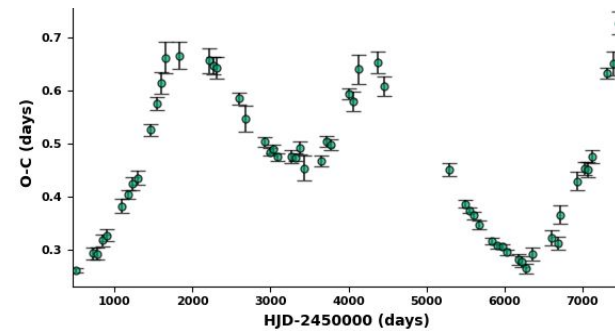
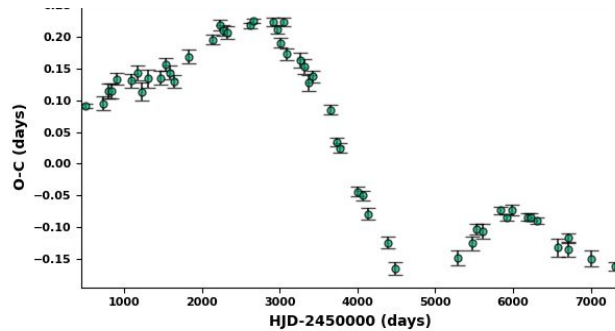
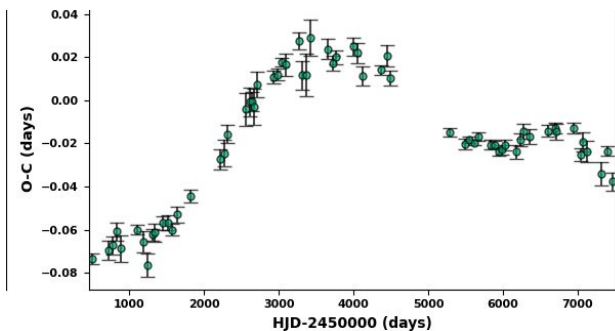


# LINEAR PERIOD CHANGE CANDIDATES

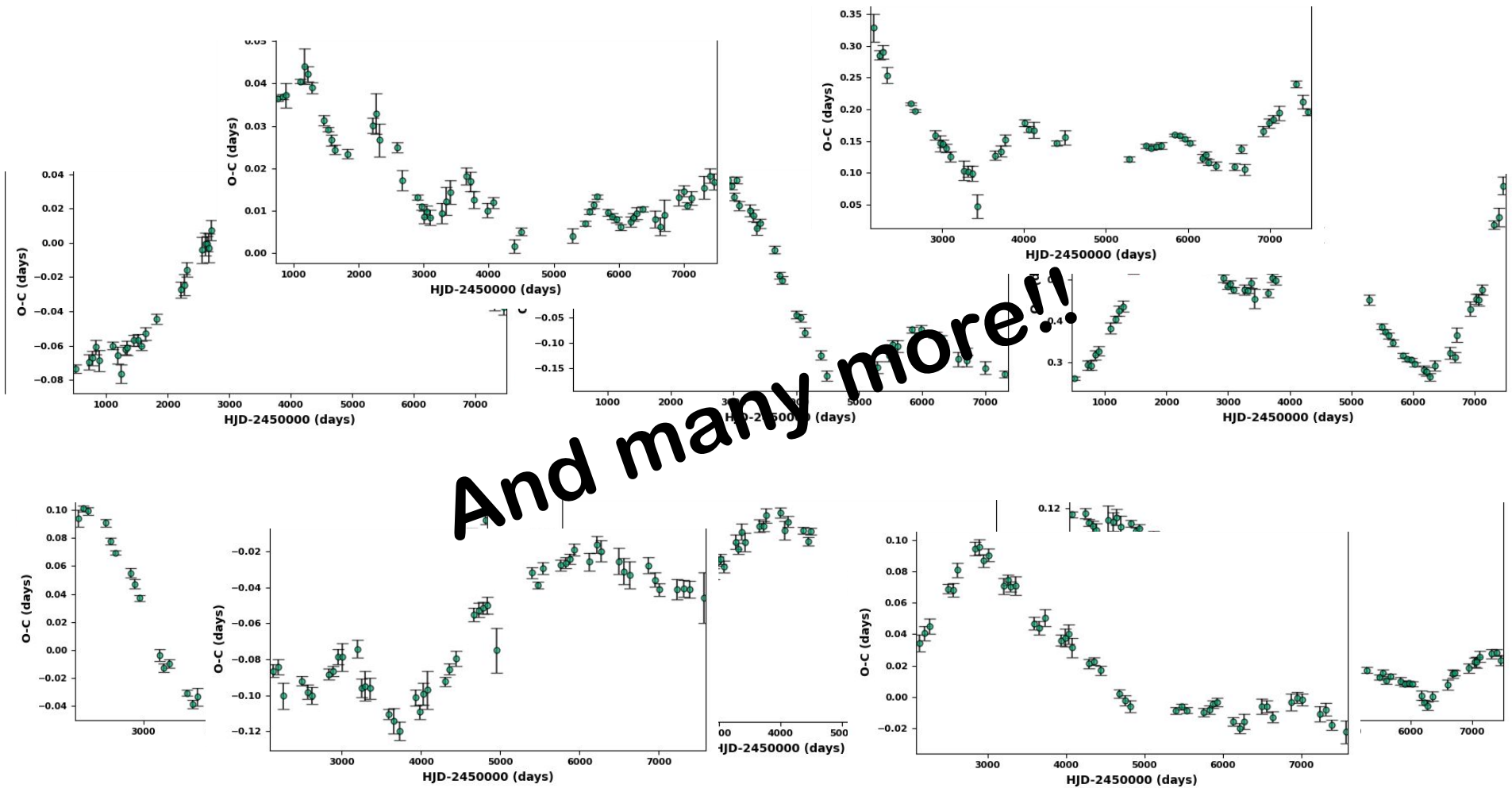


- Crossing predictions (Turner 2006)
- Time base small to capture evolutionary period change rates
- However, could capture first crossing candidates.
- We have ~10 such candidates

# IRREGULAR PERIOD CHANGE CANDIDATES



Rathour et al. 2023(b) (in prep.)



# STATISTICS

|           | <u>No PC</u> | <u>Linear PC</u> | <u>Non-Linear PC</u> |
|-----------|--------------|------------------|----------------------|
| LMC F     | 648          | 549              | 594                  |
| LMC 10    | 113          | 289              | 802                  |
| SMC F     | 941          | 557              | 982                  |
| SMC 10    | 105          | 297              | 1177                 |
| Fraction: | ~25.5 %      | ~24.2 %          | <b>~50.3 %</b>       |

- Irregular PC candidates are more in overtone Cepheids
- Lower metallicity seems to favour irregular PC

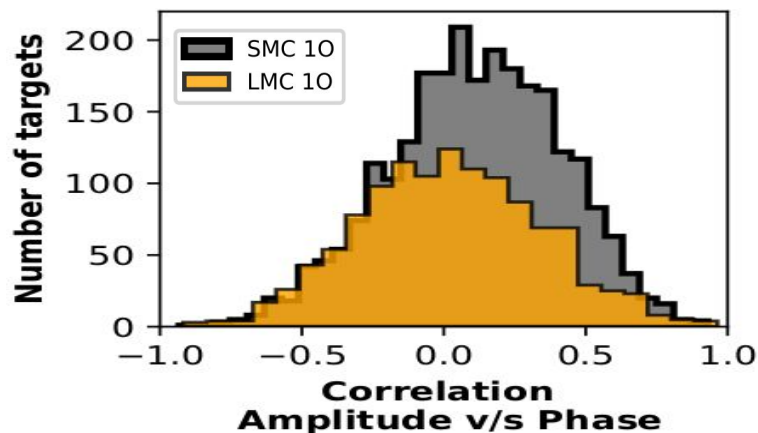
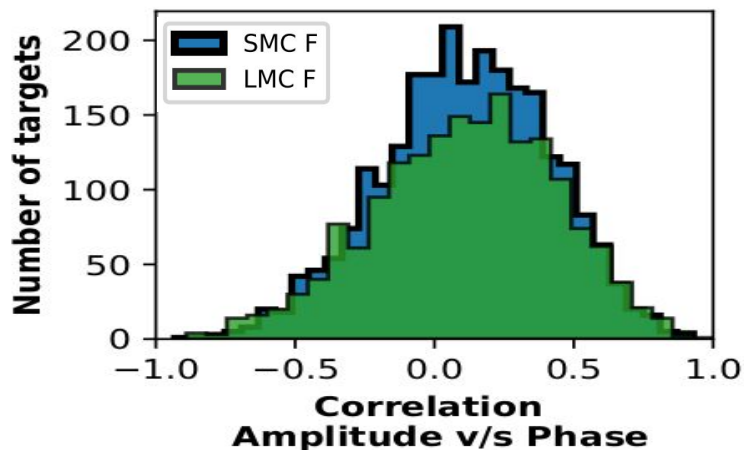
## Sample retained

LMC: ~69% (F); ~89% (10)

SMC: ~67% (F); ~94% (10)

IrPC Fraction: **~41 %**

# Effects on Period change



Rathour et al. 2023(b) (in prep.)

Large fraction of the sample has no correlation between amplitude and phase changes

# CONCLUSIONS & FUTURE WORK

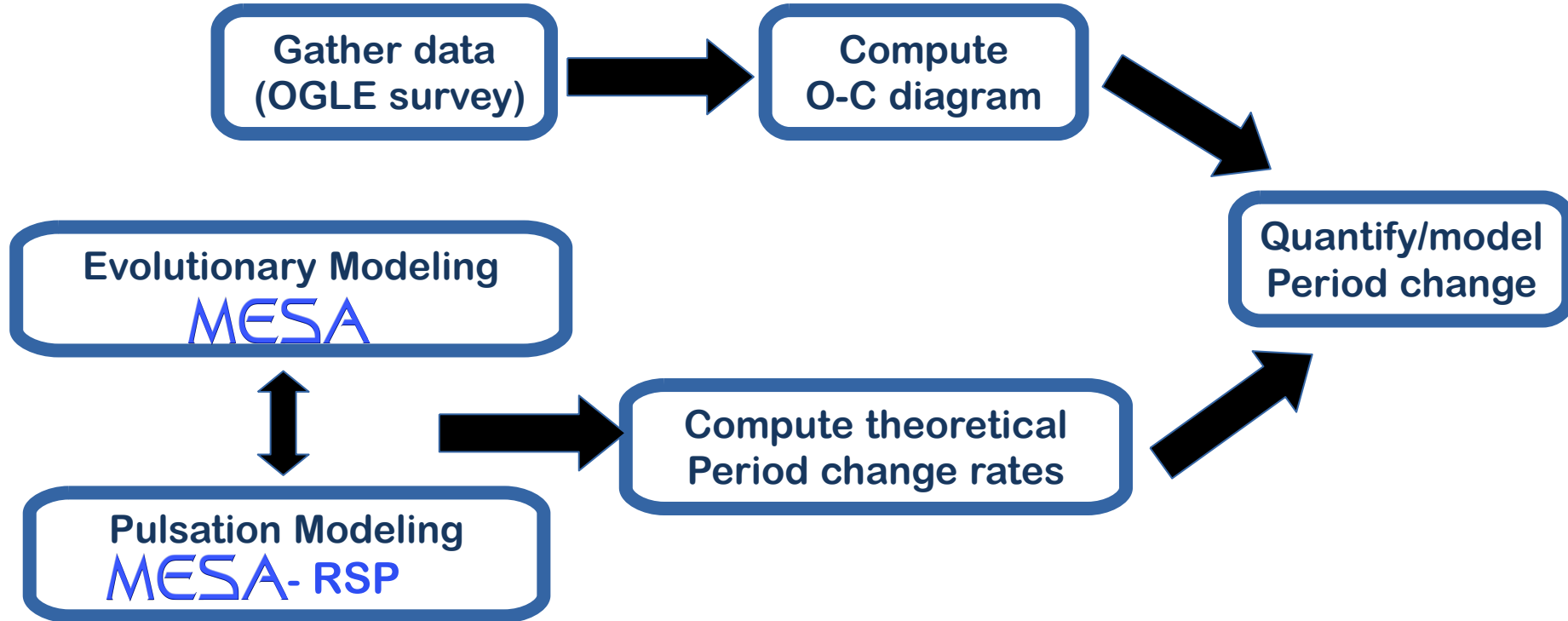
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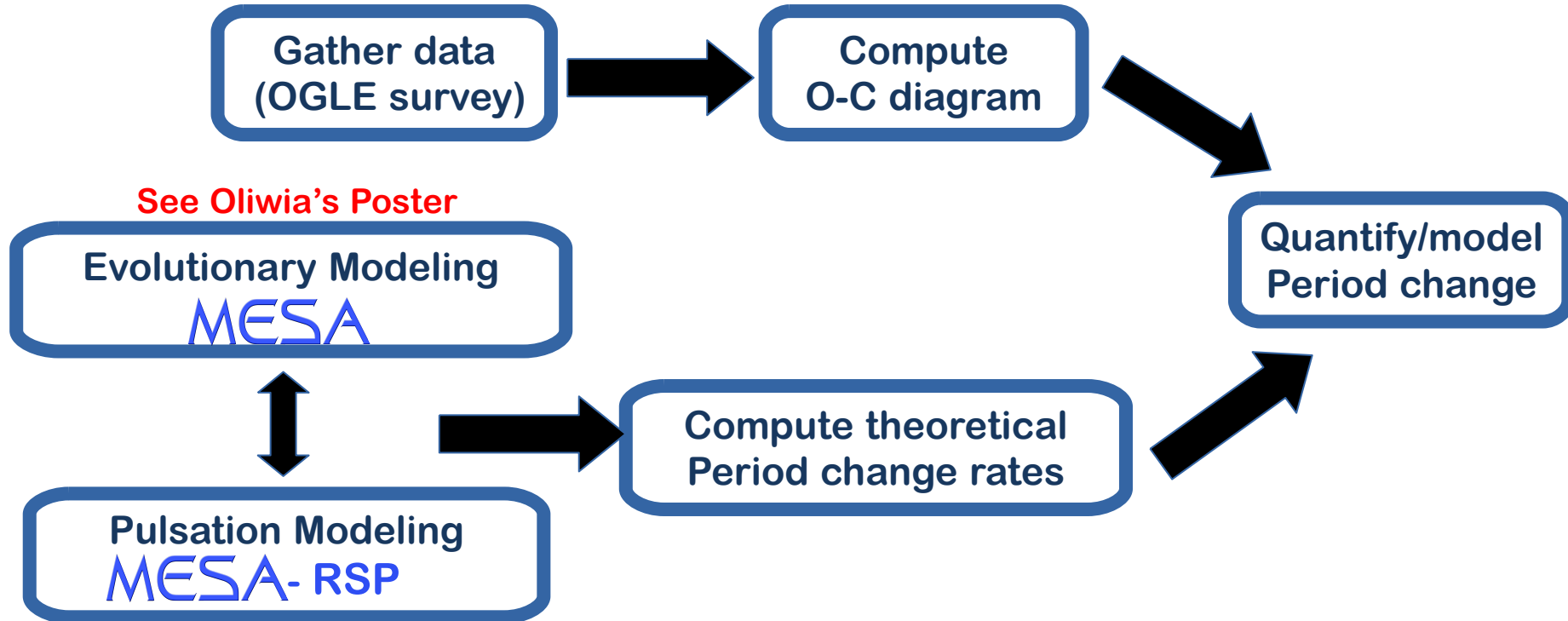
# Conclusions

- Successfully search 7200+ OGLE Magellanic Cepheids for (i) binarity and (ii) irregular period change candidates
- We find 197 Cepheid binary candidates available for the community to confirm spectroscopically. 2 SMC Cepheids with likely giant companion!
- Irregular period change: substantial fraction (upto ~40%), more likely in overtone Cepheids (Poleski 2008), and SMC (Deasy 1985), uncorrelated with amplitude changes. Fluctuations increase with period (Csörnyei et al. 2021)
- PC (evo+non-evo) are essential to understand full picture of Cepheid evolution.
- Modelling survey (MESA+RSP) with above empirical constraints.

# Future/On-going work



# Future/On-going work



**Thank you for your attention!**

**Dziękuję za uwagę!**

# APPENDIX

# What is O-C diagram?

Observed-Calculated

## What does it do?

Measures period changes rate (PCR)

$$T_{\max} = T_0 + PE$$

$$T_m = T_0 + P_0E + \frac{1}{2} \frac{dP}{dt} \bar{P} E^2$$

$$O - C = \frac{1}{2} \frac{dP}{dt} \bar{P} E^2$$

## Why is it important?

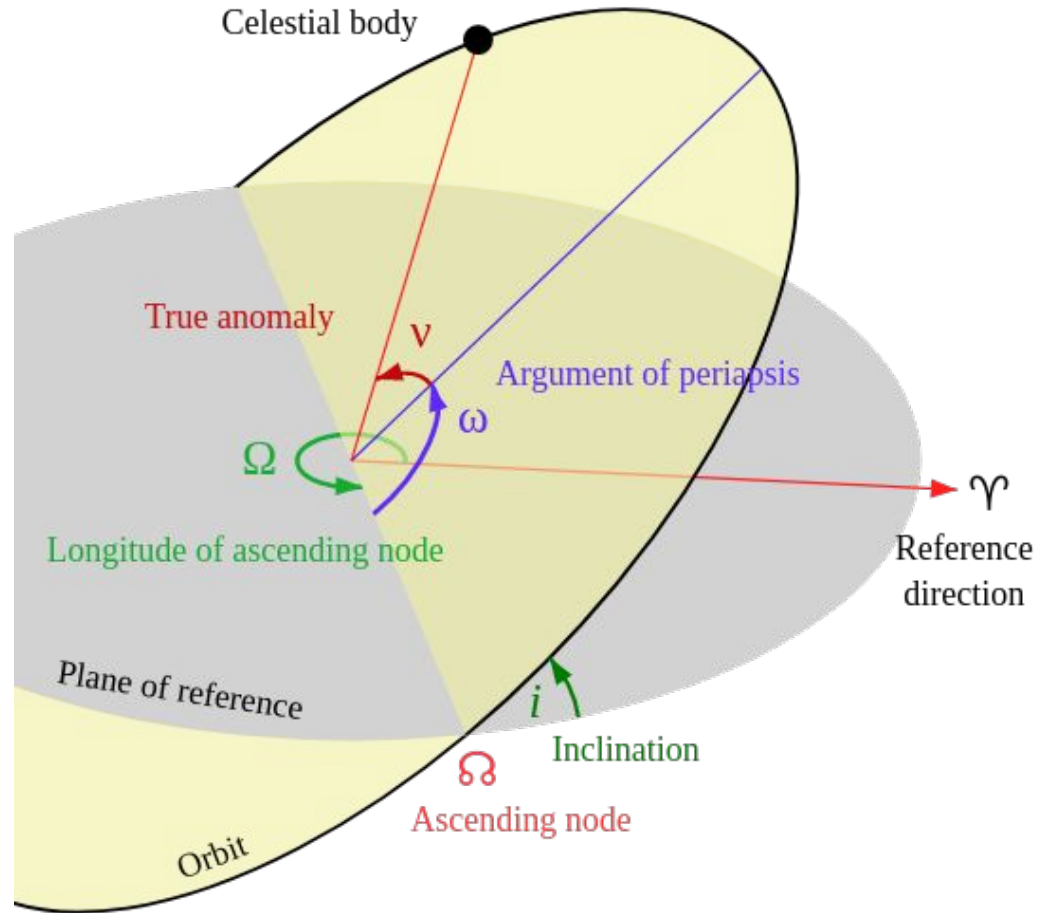
Can be a direct measure of Cepheid evolutionary and non-evolutionary processes

$$z(t) = a_1 \sin i \frac{1 - e^2}{1 + e \cos(\nu)} \sin(\nu + \omega),$$

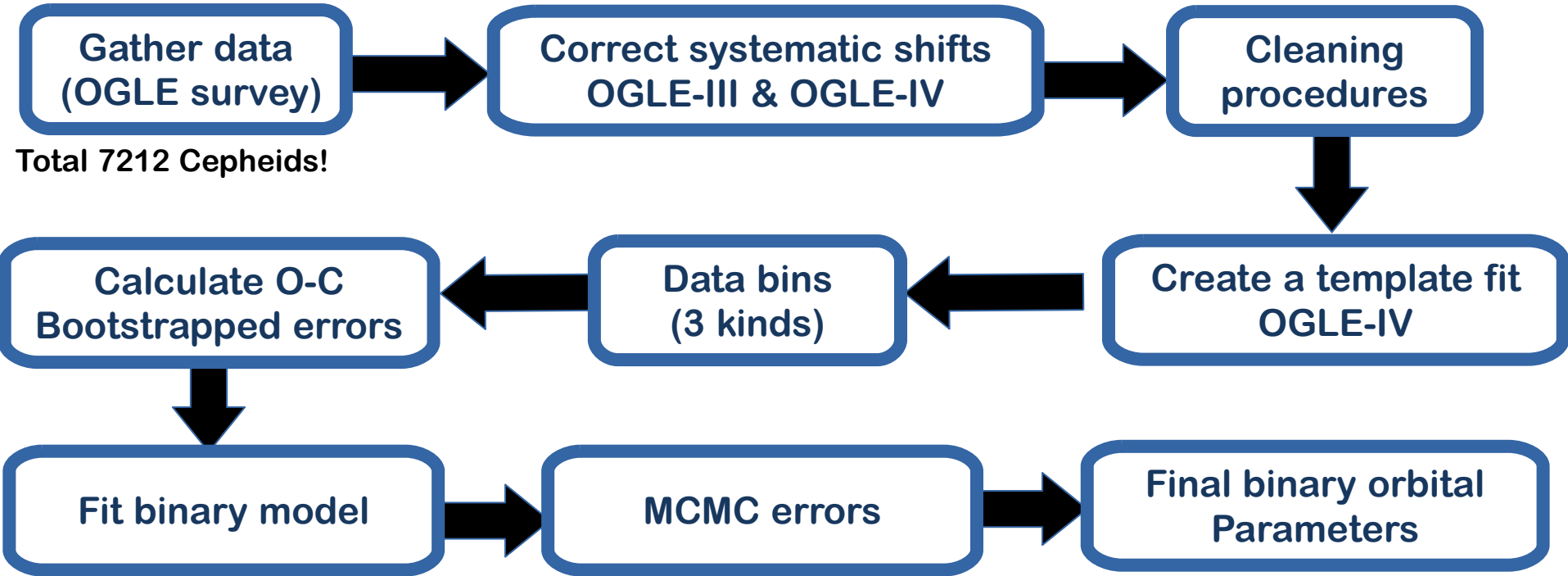
$$(O - C)(t) = z(t) + c_0 + c_1 t + c_2 t^2,$$

$$f(m) = \frac{a_1^3 \sin^3 i}{P_{\text{orb}} \sqrt{1 - e^2}},$$

$$f(m) = \frac{m_S^3 \sin^3 i}{(m_{\text{RR}} + m_S)^2},$$



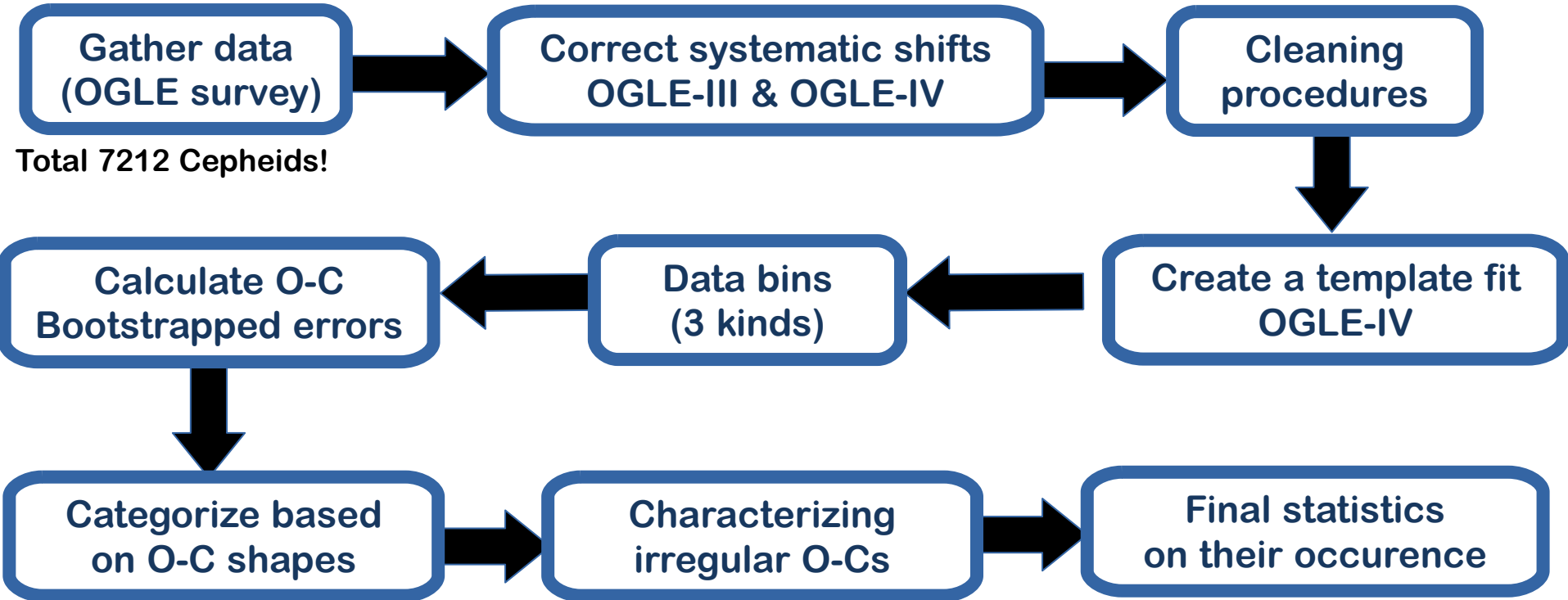
# Work flow



Code routines adapted from `rrl_binaries_1`: G. Hajdu et al. (2021)



# Work flow



# **FACTORS AFFECTING!**

**Sample was composed for Cepheids with data in both OGLE-III & OGLE-IV**

**Some candidates were rejected due to not enough LTTE O-C cycles to be convincing**

**Low amplitude noisy O-C curves were rejected**

# **METHODOLOGY: SEARCHING THE SURVEY**

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# The Optical Gravitational Lensing Experiment (OGLE)

- Largest database for variable stars!
- 1.3 m telescope, Las Campanas, Chile
- Mosaic CCD camera; FOV 1.4 square degrees
- Optical and Infra-red bands
- More than 20 years of photometry data
- OGLE-III:2001-2009 & OGLE-IV:2010-present
- Technical upgrades from OGLE-III to OGLE-IV



# OGLE SURVEY

Magellanic Cloud (MC) observed by OGLE

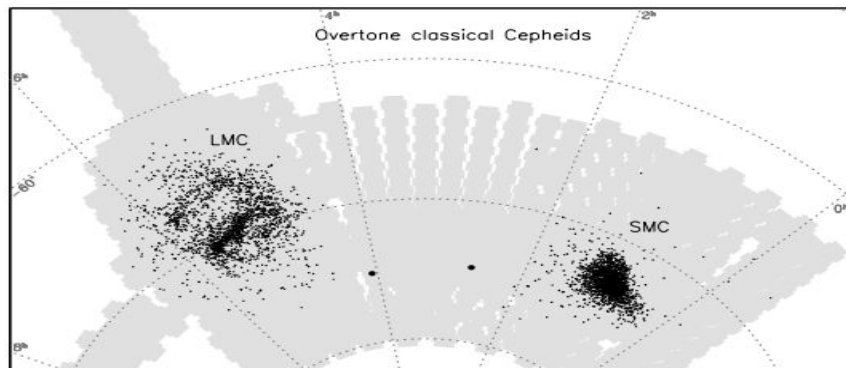
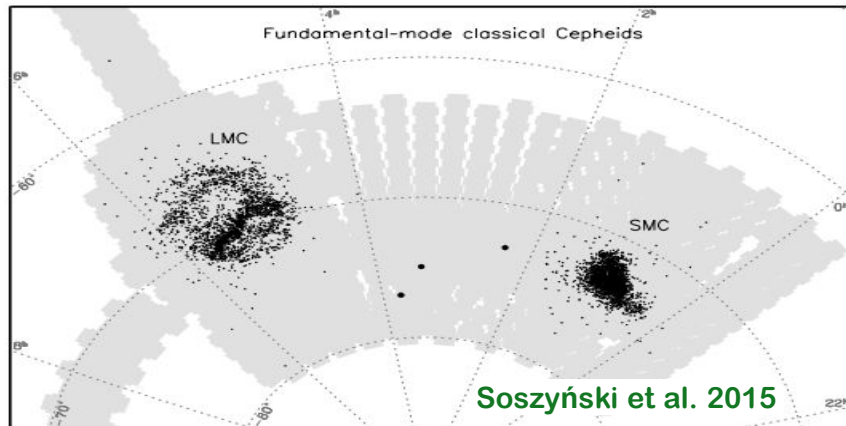
Completeness near 100% (Soszyński et al. 2017)

Our starting sample was 9649 Cepheids

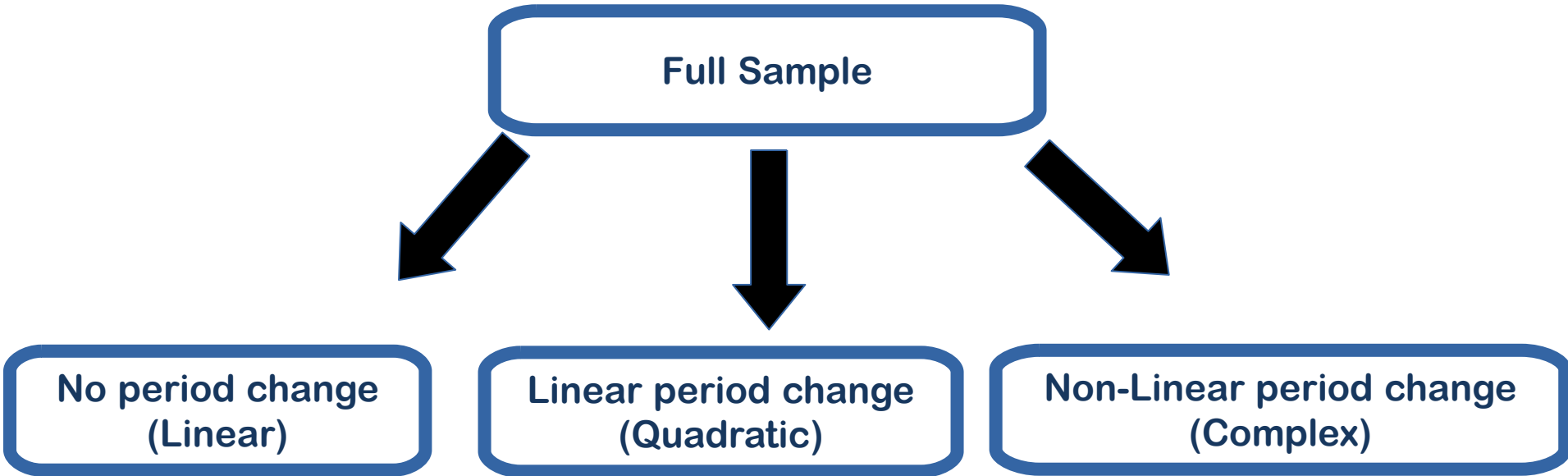
Total working sample was 7212!

Typically OGLE-III & OGLE-IV combined has 14 seasons of data

For some promising candidates, OGLE team provided extended data on request



# Filtering Process

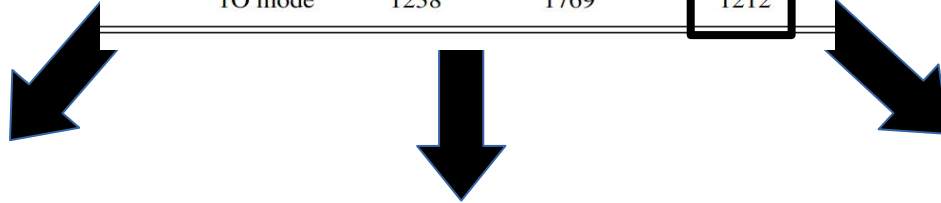


Data flag tests: AIC, BIC, Jurcsik test, reduced Chi square

Residual flag tests: Ljung-Box, Anderson-Darling

# Filtering Process

| Field | Pulsation | OGLE-III | OGLE-IV | OGLE-III+IV |
|-------|-----------|----------|---------|-------------|
| SMC   | F mode    | 2626     | 2739    | 2582        |
|       | 1O mode   | 1644     | 1790    | 1617        |
| LMC   | F mode    | 1818     | 2430    | 1801        |
|       | 1O mode   | 1238     | 1769    | 1212        |



No period change  
(Linear)

Linear period change  
(Quadratic)

Non-Linear period change  
(Complex)

Data flag tests: AIC, BIC, Jurcsik test, reduced Chi square

Residual flag tests: Ljung–Box, Anderson–Darling

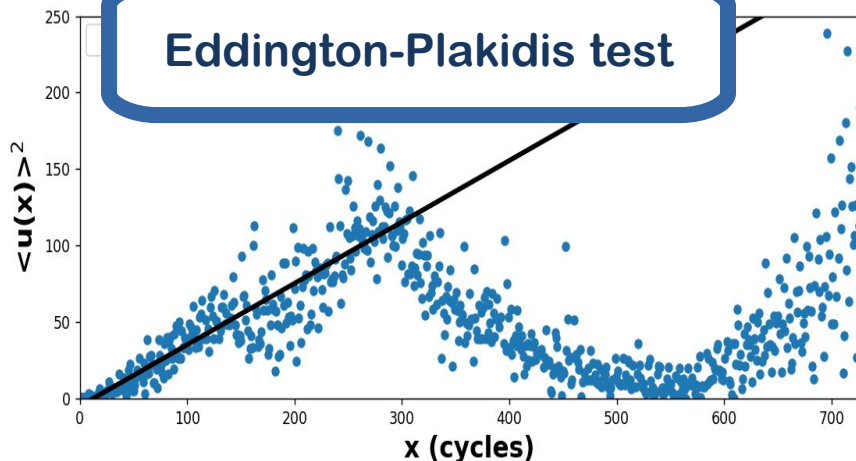
# Validating Period changes with fluctuation tests

Sample retained

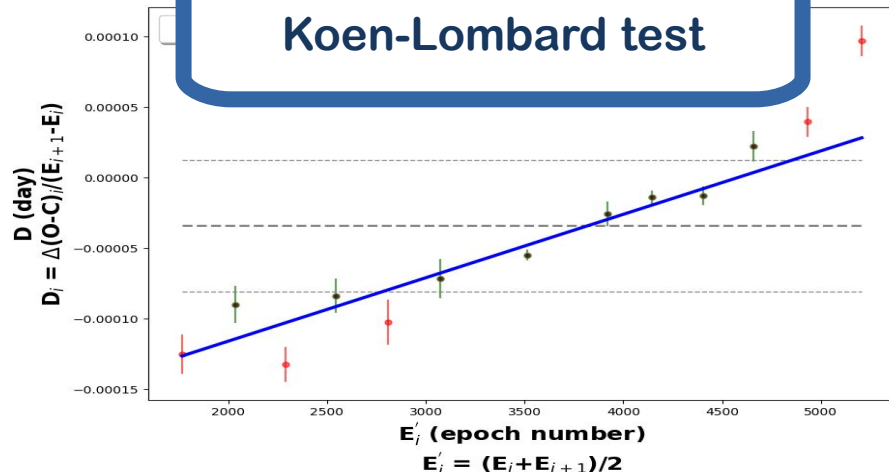
LMC: ~69% (F); ~89% (10)

SMC: ~67% (F); ~94% (10)

Eddington-Plakidis test



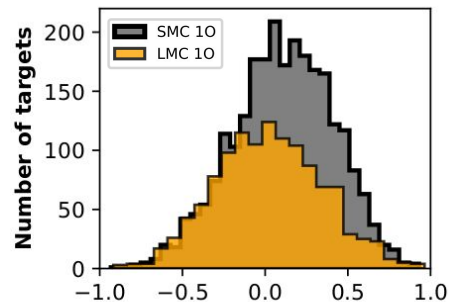
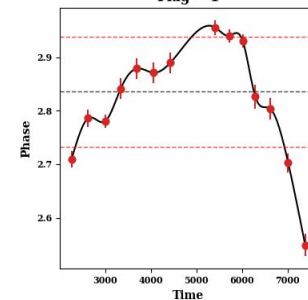
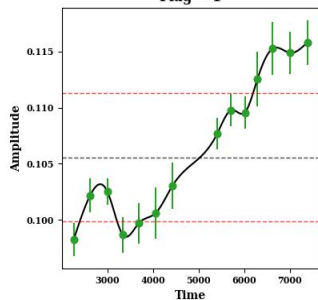
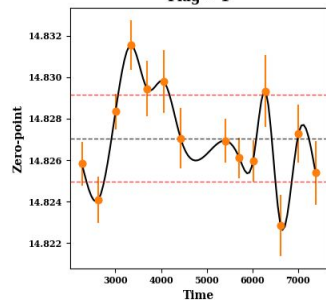
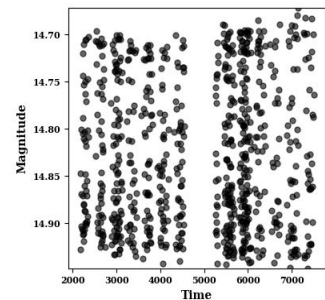
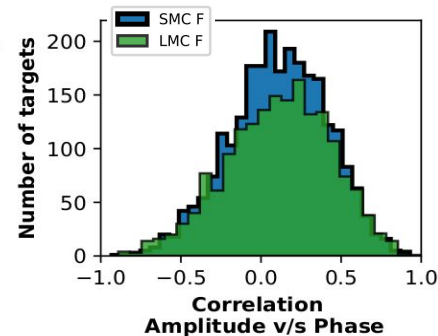
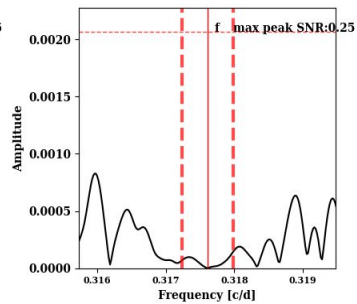
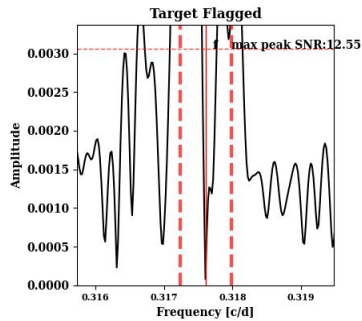
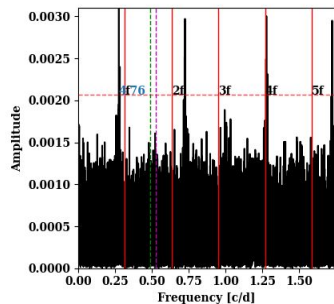
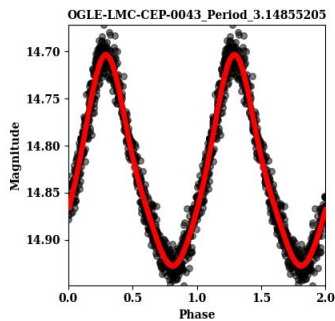
Koen-Lombard test



$E'_i = (E_i + E_{i+1})/2$   
Rathour et al. 2023(b) (in prep.)

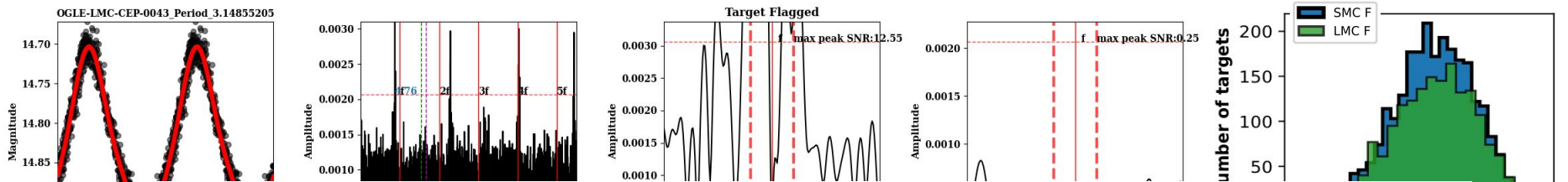


# Other effects on Period change

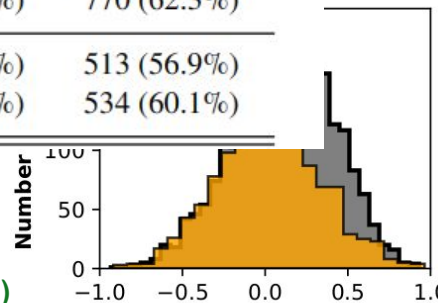
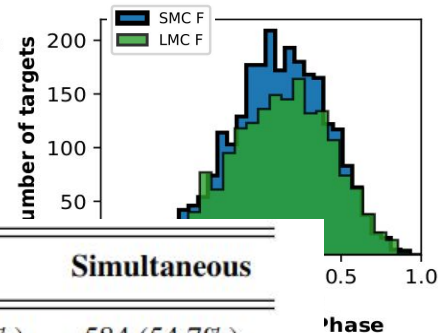
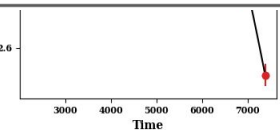
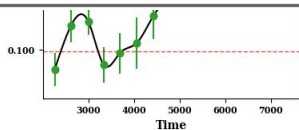
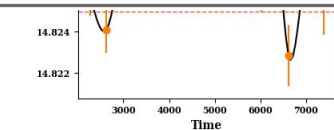
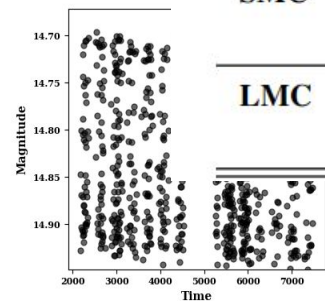


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# Other effects on Period change



| Field | Pulsation | Total | Flag 1       | Zero-point   | Amplitude    | Phase       | Simultaneous |
|-------|-----------|-------|--------------|--------------|--------------|-------------|--------------|
| SMC   | F mode    | 2526  | 1068 (42.3%) | 959 (89.8%)  | 1000 (93.6%) | 637 (59.6%) | 584 (54.7%)  |
|       | IO mode   | 1596  | 1237 (77.5%) | 1154 (93.3%) | 1042 (84.2%) | 917 (74.1%) | 770 (62.3%)  |
| LMC   | F mode    | 1780  | 1093 (61.4%) | 982 (89.8%)  | 994 (90.9%)  | 564 (51.6%) | 513 (56.9%)  |
|       | IO mode   | 1204  | 889 (73.8%)  | 839 (94.4%)  | 753 (84.7%)  | 631 (71.0%) | 534 (60.1%)  |



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# Modeling Work Plan

MESA

Compute Evo tracks grid  
(overshooting, mass-loss)



MESA-RSP

Compute Pul model  
(M, L, T, X, Z,  $\alpha$ )



Calculate theoretical  
Period change rates



Compare with observations  
(P, PCR, RV, LC)

# (Un)Knowns about evolutionary PCR

- 67% inc. and 33% dec. PCR (Turner 2006)
- Overtone pulsation less stable (Poleski 2008)
- Reasonable agreement with theoretical models yet cannot satisfactorily reproduce PCR distribution

# (Un)knowns about non-evolutionary PCR

- Least in galactic field; More likely to be in SMC (Deasy 1985) (Perhaps, a metallicity trend ?)
- Lack of systematic search and mechanism.

# Validating Period changes with fluctuation tests

**Sample retained**

**LMC: ~69% (F); ~89% (10)**

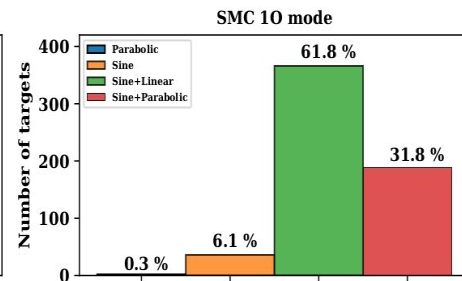
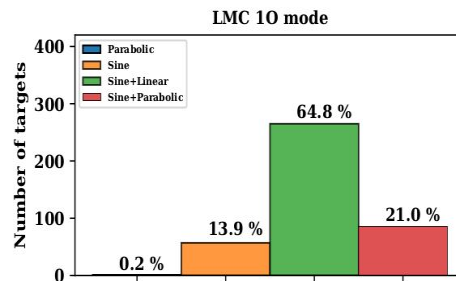
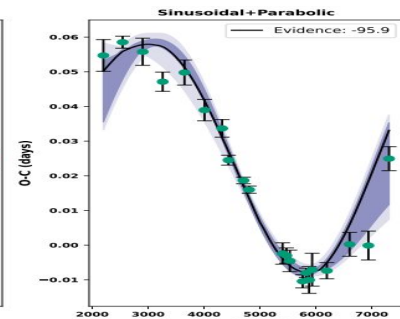
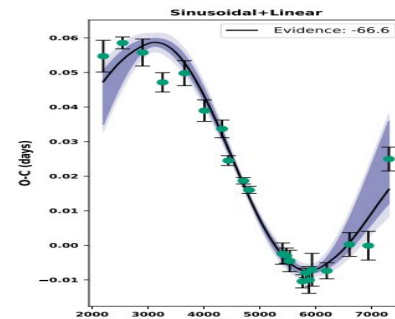
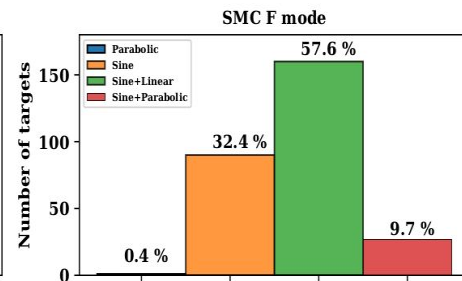
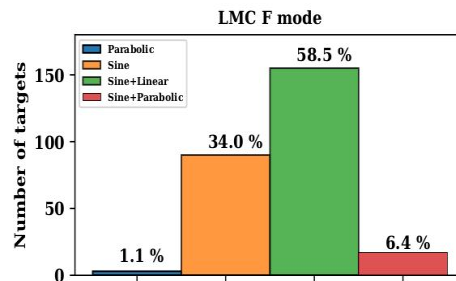
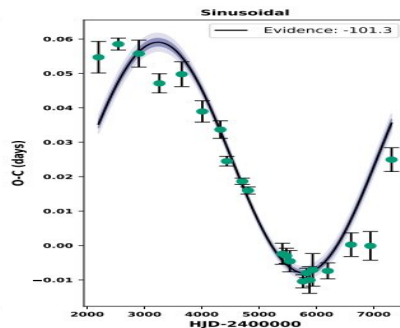
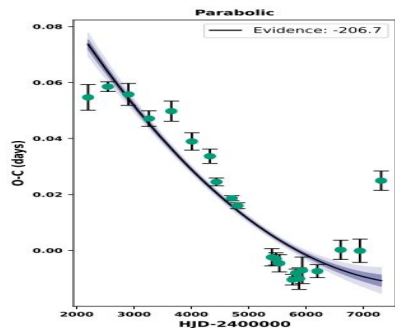
**SMC: ~67% (F); ~94% (10)**

**Occurance rate:**

**LMC: ~10.3% (F); ~58.8% (10)**

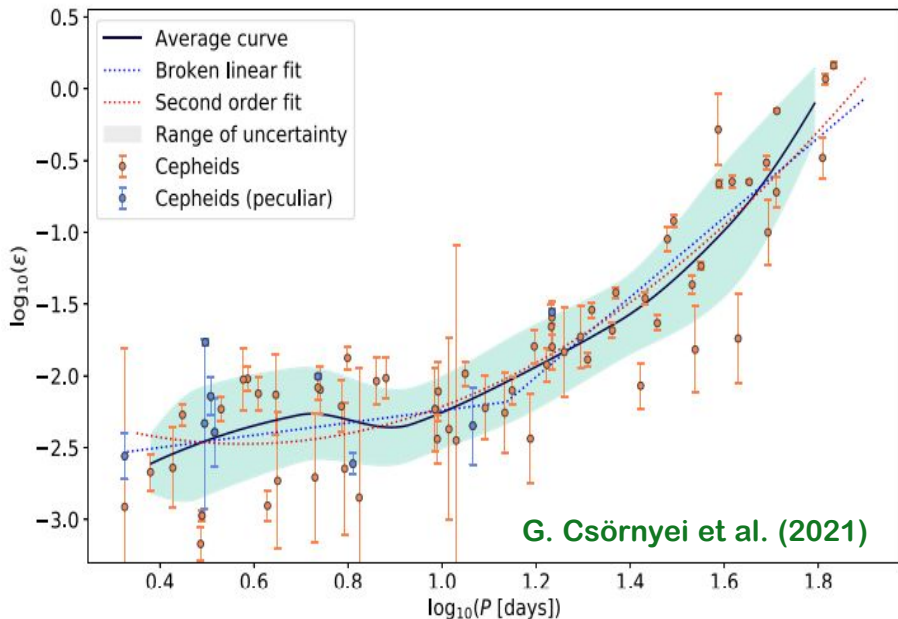
**SMC: ~14.4% (F); ~68.4% (10)**

| Field | Pulsation | OGLE-III | OGLE-IV | OGLE-III+IV |
|-------|-----------|----------|---------|-------------|
| SMC   | F mode    | 2626     | 2739    | 2582        |
|       | 10 mode   | 1644     | 1790    | 1617        |
| LMC   | F mode    | 1818     | 2430    | 1801        |
|       | 10 mode   | 1238     | 1769    | 1212        |



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# Validating Period changes with fluctuation tests



Sample retained

LMC: ~69% (F); ~89% (10)

SMC: ~67% (F); ~94% (10)

IrPC Fraction: **~41 %**

